

**Note:** You'll want to read Chapter 2 of Vershynin, especially Section 2.4, before answering these problems.

**Vershynin 2.4.2** Consider the random graph  $G \sim G(n, p)$  with expected degrees  $d \leq C \log n$  for some constant  $C \geq 1$ . Show that with high probability (say 0.9), all the vertices of  $G$  have degree  $\mathcal{O}(\log n)$ .

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**Vershynin 2.4.3** Consider the random graph  $G \sim G(n, p)$  with expected degrees  $d \leq C$  for some constant  $C > 1$ . Show that with high probability (say 0.9), all the vertices of  $G$  have degree  $\mathcal{O}\left(\frac{\log n}{\log \log n}\right)$ .

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